Slides: http://tinyurl.com/ksb32xw

**How to use SMT** 

http://rise4fun.com/z3py/tutorial

http://stackoverflow.com/users/2327608/juan-ospina?tab=questions&sort=activity

## **Pencil and paper**

- 1) Find the conditions on a, b s.t.  $a x^4 + a x^3 + b x^2 + (a + b) < 0$
- 2) Prove Sturm's Theorem. Hint: break interval (a, b) into fundamental intervals:

$$(a = a_0, a_1), (a_1, a_2), ..., (a_{m-1}, a_m = b)$$

Each interval contains at most one root of  $h_0$ ,  $h_1$ , ...,  $h_n$ 

If  $h_n$  is not a constant polynomial, consider the sequence  $\widehat{h_i} = \frac{h_i}{h_n}$ 

## **Programming**

- 1) Implement the basic operations  $(+,\times,...)$  for univariate polynomials. Suggestion: represent polynomials using list (or vector) of coefficients.
- 2) Implement the Polynomial division algorithm for univariate polynomials.
- 3) Use to implement Sturm's sequences, and find the number of roots.